

I.

$$A \cdot \vec{x} = \vec{b}$$

$$|A|^{-1}$$

$$\vec{x} = A^{-1} \cdot \vec{b}$$

1.  $\det(A) \neq 0$   
invertierbar

2.  $A_{11} \dots A_{nn}$

3. Vektorprodukte  
(äußer)

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II.

$$\det(A - \lambda E) = 0$$

Eigenwerte

$$A \cdot \vec{x} = \lambda \cdot \vec{x}$$

$$3) \text{ Eigenwerte: } \det(A - \lambda \cdot E) = 0$$

$$\begin{array}{r} (-\lambda^3 + 5\lambda^2 - 2\lambda - 8)(\lambda + 1) = -\lambda^2 + 6\lambda - 8 \\ \underline{-(-\lambda^3 - \lambda^2)} \\ -6\lambda^2 - 2\lambda - 8 \\ \underline{-(-6\lambda^2 + 6\lambda)} \\ -8\lambda - 8 \\ \underline{-(-8\lambda - 8)} \\ - \end{array} \quad \begin{array}{l} -(\lambda^2 - 6\lambda + 8) \\ -(\lambda - 4)(\lambda - 2) \end{array}$$

$$\lambda = \{-1; 2; 4\}$$

$$A \cdot \vec{x} = \lambda \cdot \vec{x}$$

$$\lambda = 2 \quad : \quad \begin{pmatrix} 2 & 1 & 2 \\ 2 & 2 & -2 \\ 3 & 1 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \Rightarrow \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

$$\left\{ \begin{array}{l} 2x_1 + x_2 + 2x_3 = 2x_1 \\ 2x_1 + 2x_2 - 2x_3 = 2x_2 \\ 3x_1 + x_2 + x_3 = 2x_3 \end{array} \right. \rightarrow \left\{ \begin{array}{l} x_2 + 2x_3 = 0 \\ 2x_1 - 2x_3 = 0 \\ 3x_1 + x_2 - x_3 = 0 \end{array} \right.$$

$$\left. \begin{array}{l} x_2 = -2x_3 \\ x_1 = x_3 \\ x_3 = \beta \end{array} \right\} \begin{array}{l} 3x_2 - 2x_3 - x_3 = 0 \\ 0 = 0 \end{array} \downarrow$$

$$\hookrightarrow \vec{x} = \begin{pmatrix} \beta \\ -2\beta \\ \beta \end{pmatrix}$$