

$$2) \quad \ln 2^6 - \ln 2^2 \cdot x^{-2} + \ln 2^6 = \ln x^6 - \ln x^{-2} - \ln \left(\frac{1}{2^2} \right)^2$$

$$\begin{aligned} \frac{1}{2} \cdot \ln \frac{16}{x^4} &= \frac{1}{2} \cdot \ln 16x^{-4} = \ln (16x^{-4})^{\frac{1}{2}} \\ &= \ln \sqrt{16x^{-4}} = \ln 4x^{-2} = \ln 2^2 x^{-2} \end{aligned}$$

$$\rightarrow \ln \frac{2^6 \cdot 2^6}{2^2 x^{-2}} = \ln \frac{x^6}{x^{-2} \cdot \frac{1}{2^4}} \quad | \nearrow e$$

$$\frac{2^6 \cdot 2^6 \cdot x^2}{2^2} = x^6 \cdot x^2 \cdot 2^4$$

$$\frac{2^6 \cdot 2^6}{2^2 \cdot 2^4} = \frac{x^6 \cdot x^2}{x^2}$$

$$2^6$$

$$= x^6$$

$$x = 2$$

$$\Rightarrow \mathcal{K} = \{2\}$$

$$42 + \log(2 - \sqrt{x-2})$$

$$x-2=0$$

$$x=2$$

$$x=1 : 1-2 = -1 \quad \text{✗}$$

$$x=3 : 3-2 = +1 \quad \text{✓}$$

$$\Rightarrow x \geq 2$$

$$2 - \sqrt{x-2} = 0$$

$$2 = \sqrt{x-2}$$

$$4 = x-2$$

$$6 = x$$

$$x < 6$$

$$x=5 : 2 - \sqrt{3} > 0$$

$$x=7 : 2 - \sqrt{5} < 0$$

$$\mathbb{D} = \{x \in \mathbb{R} \mid x \geq 2 \wedge x < 6\}$$

$$\mathbb{K} = \mathbb{R}$$

5) $f(x) = \frac{4^x}{\ln(3x+6)}$

$3x+6=0$
 $x=-2$

$x = -1 : 3 \checkmark$
 $x = -3 : -3$

$x > -2$

$\ln(3x+6) = 0$
 $3x+6 = 2^0 = 1$
 $x = -5/3 = \boxed{-1\frac{2}{3}} = -1,6\bar{6}$

$D = \{x \in \mathbb{R} \setminus \{-1\frac{2}{3}\} \mid x > -2\}$

Mitternachtsformel

$$ax^2 + b \cdot x + c = 0 \quad | : a$$

$$x^2 + \frac{b}{a} \cdot x + \frac{c}{a} = 0$$

$$\left(x + \frac{b}{2a}\right)^2 - \left(\frac{b}{2a}\right)^2 + \frac{c}{a} = 0$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2}{4a^2} - \frac{4ac}{4a^2} = \frac{b^2 - 4ac}{4a^2} \quad | \sqrt{\quad}$$

$$\left[x^2 + 2 \cdot x \cdot \frac{b}{2a} + \left(\frac{b}{2a}\right)^2 \right] - \left(\frac{b}{2a}\right)^2 + \frac{c}{a}$$

$$x + \frac{b}{2a} = \pm \sqrt{\frac{b^2 - 4ac}{4a^2}} = \pm \frac{\sqrt{b^2 - 4ac}}{2a} \quad | - \frac{b}{2a}$$

$$x_{1/2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (a=1)$$

$$x_{1/2} = \frac{-5 \pm \sqrt{6^2 - 4c}}{2}$$

$$= -\frac{6}{2} \pm \sqrt{\frac{6^2 - 4c}{4}}$$

$$= -\frac{6}{2} \pm \sqrt{\frac{6^2}{4} - c}$$

$\left(\frac{6}{2}\right)^2$

$$1 + \left(\frac{6}{2}\right)^2 - \frac{c}{a}$$

| \sqrt{\quad}

$$5) \quad f(x) = \frac{1}{4}x^2 + 2x + 3 = \frac{1}{4}[x^2 + 8x + 12] \leftarrow \\ = \frac{1}{4}[(x+6)(x+2)]$$

Verlauf: gestaut, da $|a| < 1$
oben geöffnet, da $a > 0$

Schnittpunkte: $S_y (0|3)$; $S_{x_1} (-6|0)$; $S_{x_2} (-2|0)$

Scheitelpunkt: $\frac{1}{4}[(x+4)^2 - 4^2 + 12] = \frac{1}{4}[(x+4)^2 - 4]$

$$f(x) = \frac{1}{4}(x+4)^2 - 1 \rightarrow S(-4|1)$$

Symmetrie: Achsensymmetrie durch Parallele
zur y-Achse bei $x = -4$

$$1) \quad x^2 - 6x + 8 = 0 \quad (x-4)(x-2)$$

$$x_{1,2} = \frac{6}{2} \pm \sqrt{9-8} = 3 \pm 1 = 4; 2$$

$$2) \quad x^2 - 4x - 5 = 0 \quad (x-5)(x+1)$$

$$(x-2)^2 - 4 - 5 = (x-2)^2 - 9 = 0 \quad \mu = \{5; -1\}$$

$$(x-2)^2 = 9$$

$$x-2 = \pm 3 \quad ; \quad x = \pm 3 + 2$$

$$3) \quad x^2 - 10x + 16 = 0 \quad (x-2)(x-8)$$

$$(x-5)^2 - 25 + 16 = (x-5)^2 - 9 = 0 \quad \mu = \{8; 2\}$$

$$(x-5)^2 = 9 \quad x-5 = \pm 3 \quad x = \pm 3 + 5$$