

1) $f(x) = x^2 - x - 12$; $g(x) = 2x - 2$

2) $\int_{-1}^2 (x^3 + 4x^2 + x - 6) dx$

3) $f(x) = -3x^2 - 6x + 45$ Fläche im 1. Quadranten

4) $f(x) = 24x^3 - 24x^2 - 6 \cdot (4x - 4)$ Fläche mit der
x-Achse

5) $f(x) = x^3 - 6x^2 + 8x + 5$

Fläche der Wendetangente im 1. Quadranten

a) mittels Integral

b) ohne Integral

$$1) \frac{343}{6}$$

$$2) f(x) = x^3 + 4x^2 + x - 6 = (x-1)(x+2)(x+3)$$

$$\int_{-1}^2 f(x) dx = \int_{-1}^1 f(x) dx + \int_1^2 f(x) dx$$

$$F(x) = \frac{1}{4}x^4 + \frac{4}{3}x^3 + \frac{1}{2}x^2 - 6x$$

$$F(-1) = \frac{1}{4} - \frac{4}{3} + \frac{1}{2} + 6 = \frac{3 - 16 + 6 + 72}{12} = \frac{65}{12}$$

$$F(1) = \frac{1}{4} + \frac{4}{3} + \frac{1}{2} - 6 = \frac{3 + 16 + 6 - 72}{12} = -\frac{47}{12}$$

$$F(2) = \frac{16}{4} + \frac{32}{3} + \frac{4}{2} - 12 = \frac{48 + 128 + 24 - 144}{12} = \frac{56}{12}$$

$$\int_{-1}^2 f(x) dx = |F(1) - F(-1)| + |F(2) - F(1)|$$
$$= \left| -\frac{47}{12} - \frac{65}{12} \right| + \left| \frac{56}{12} - \left(-\frac{47}{12}\right) \right|$$

$$\frac{112}{12} + \frac{103}{12} = \frac{215}{12} \text{ FE}$$