

$$1) \sum (-1)^{k+1} \cdot \frac{\sqrt{k+1}}{k} \cdot 42$$

$$2) \sum \frac{(k+1) \cdot 3^k}{(2k+1)!}$$

$$3) \sum \frac{\sin^k(k)}{(3+k)^k}$$

$$4) \sum \frac{k^2 \cdot 5^k}{(3k)!}$$

$$5) \sum (-3)^{2k+1} \cdot \frac{2}{3^{4k}}$$

$$6) \sum_{k=3}^5 \frac{1}{4} \cdot (2)^{-2k}$$

$$7) \sum_{k=2}^8 \frac{2^{2k+1}}{3k!}$$

$$8) \sum_{k=2}^8 (-1)^{k+1} \cdot \frac{2 \cdot 4^k}{(2k+1)!}$$

$$9) \sum_{k=3}^8 \left(\left(\frac{1}{3}\right)^{2k} - \left(\frac{2}{k}\right)^2 \right)$$

} Wert der Reihe
→

1) Leibniz, da $(-1)^{k+1}$ alternierend ist.

$$42. \sum \underline{(-1)^{k+1}} \cdot \frac{\sqrt{k+1}}{k} \Rightarrow \lim_{k \rightarrow \infty} \frac{\sqrt{k+1}}{k} = \lim_{k \rightarrow \infty} \frac{\sqrt{k+1}}{\sqrt{k^2}}$$

Konvergenz \Leftarrow $\lim_{k \rightarrow \infty} \sqrt{\frac{k+1}{k^2}} = \lim_{k \rightarrow \infty} \sqrt{\frac{k \cdot (1 + \frac{1}{k})}{k^2}} = 0$

2) $\sum \frac{(k+1) \cdot 3^k}{(2k+1)!} \Rightarrow$ Quotientensatz, da "!"

$$\lim_{k \rightarrow \infty} \frac{a_{k+1}}{a_k} = \lim_{k \rightarrow \infty} \frac{\underbrace{((k+1)!) \cdot 3^{k+1}}_{a_{k+1}} \cdot \underbrace{(2k+1)!}_{1/a_k}}{3^k \cdot (k+1)}$$

$$\lim_{k \rightarrow \infty} \frac{3^{k+1} \cdot (k+2) \cdot (2k+1)!}{3^k \cdot (k+1) \cdot (2k+1)! \cdot (2k+3) \cdot (2k+2)} = \lim_{k \rightarrow \infty} \frac{3 \cdot (k+2)}{(k+1) \cdot (2k+3) \cdot (2k+2)}$$

$$\lim_{k \rightarrow \infty} \frac{3 \cdot \overbrace{k(1 + \frac{2}{k})}^0}{\overbrace{k \cdot (1 + \frac{1}{k})}^0 \cdot (2k+3) \cdot (2k+2)} = \left[\frac{3}{1 \cdot (2k+3) \cdot (2k+2)} \right] = 0 < 1$$

$$3) \sum \frac{\sin^k(k)}{(3+k)^k} \Rightarrow \text{Wurzelsatz}$$

$$\lim_{k \rightarrow \infty} \sqrt[k]{\frac{\sin^k(k)}{(3+k)^k}} = \lim_{k \rightarrow \infty} \frac{|\sin(k)|}{3+k} = \left[\frac{[-1; 1]}{3+k} \right] = 0 < 1$$

$$5) \sum (-3)^{2k+1} \cdot \frac{2}{3^{4k}} = \sum (-1)^{2k+1} \cdot 3^{2k+1} \cdot \frac{2}{3^{4k}}$$

$$= \sum \underbrace{(-1)}_{-1} \cdot \underbrace{3^{0k} \cdot 3^1}_{3} \cdot \frac{2}{3^{4k}}$$

$$= -6 \cdot \sum \frac{3^{2k}}{3^{4k}} = -6 \cdot \sum \left(\frac{3^2}{3^4} \right)^k = -6 \cdot \sum \left(\frac{1}{3} \right)^k$$

$\sum q^k$ ist konvergent, wenn $|q| < 1$ \downarrow $q = \frac{1}{3} < 1$ ✓

$$\lim_{k \rightarrow \infty} \sqrt[k]{\left| \left(\frac{1}{3} \right)^k \right|} = \frac{1}{3} < 1 \quad \underline{\text{Konvergent}}$$