

$$f(x) = x^2$$

$$\# = \{(x; y) \in \mathbb{R} \times \mathbb{R} \mid y = x^2\}$$

$$\#^* = \{(x; y) \in \mathbb{R}_0^+ \times \mathbb{R}_0^+ \mid y = x^2\}$$

$$\#^{-1} = \{(x; y) \in \mathbb{R}_0^+ \times \mathbb{R}_0^+ \mid y = \sqrt{x}\}$$

$$y = +\sqrt{x}$$

$$\sqrt{3x-1} = 2x+7$$

↓

2 Lösungen x_1 ; x_2

↓ Probe $\oplus \sqrt{x}$

1 Lösung

$$x^2 - 3 = 1 \quad | +3$$

$$x^2 = 4 \quad | \sqrt{\quad}$$

$$x_{1/2} = \pm \sqrt{4}$$

$$x_{1/2} = \pm 2$$

$$2011-1 : A = \{ \underline{1}; 2; \underline{3}; 4; 6; 8; 10; 12 \}$$

$$B = \{ \underline{1}; \underline{3}; 5; 7; 9; 11; 13 \}$$

$$a) A \cap B = \{ 1, 3 \} = \{ x \in \mathbb{N}^{\leq 3} \mid x \bmod 2 \neq 0 \}$$

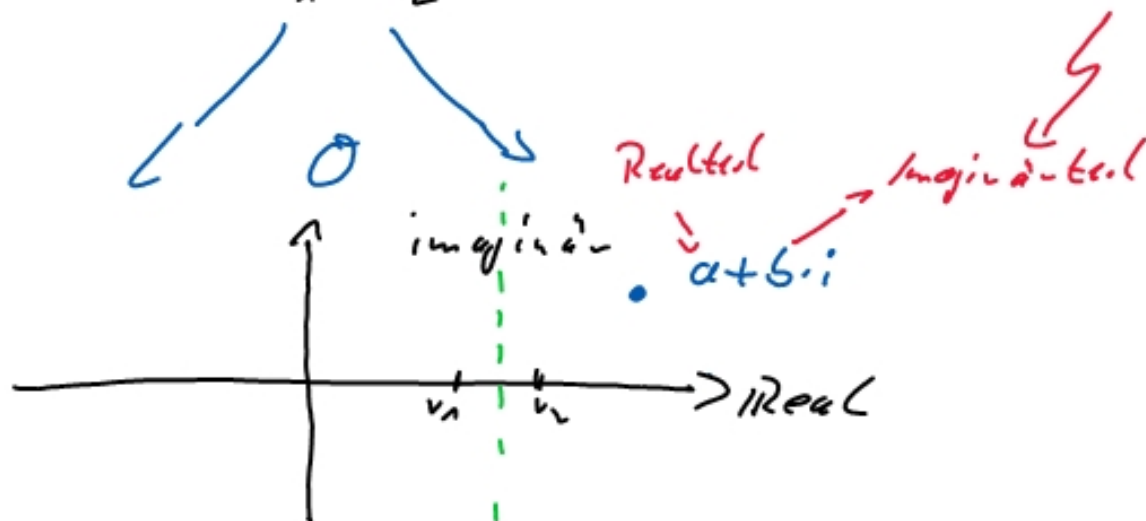
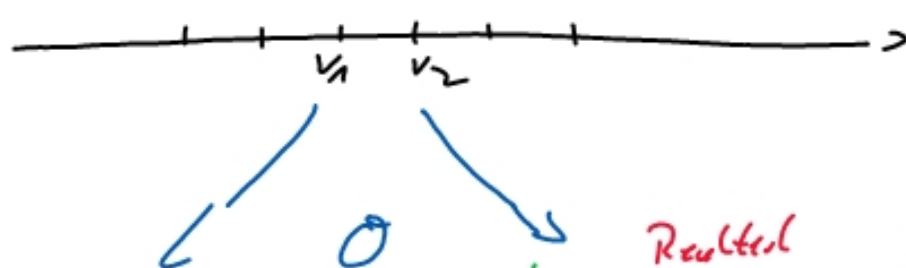
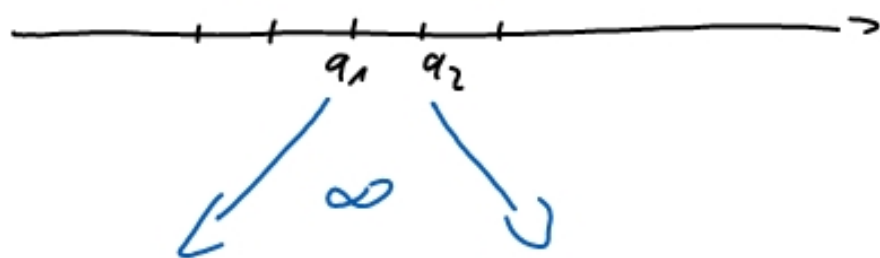
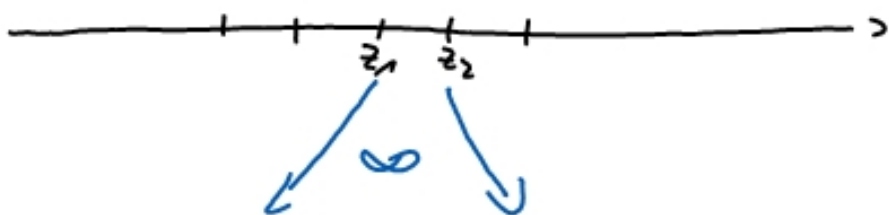
$$b) A \cup B = x \in [1; 13]_{\mathbb{N}}$$

$$c) A \setminus B = \{ x \in \mathbb{N}^{\leq 12} \mid x \bmod 2 = 0 \}$$

$$d) B \setminus A = \{ x \in [5; 13]_{\mathbb{N}} \mid x \bmod 2 \neq 0 \}$$

Komplexe Zahlen $z = a + b \cdot i$; $i = \sqrt{-1}$

\mathbb{Z}
↓
 \mathbb{Q}
↓
 \mathbb{R}
↓
 \mathbb{C}



$$j = \sqrt{-1} \Rightarrow j^2 = -1$$



$$\begin{aligned} 1) \quad & (2i - 5) - 3 \cdot (2 - i) \\ & 2i - 5 - 6 + 3i = -11 + 5i \end{aligned}$$

$$\begin{aligned} 2) \quad & -4i \cdot (3i - 5) - 2 \cdot (4i + 2) \cdot (3 - 2i) \\ & -12i^2 + 20i - 2 \cdot (12i - 8i^2 + 6 - 4i) \end{aligned}$$

$$\hookrightarrow + (-8i - 4) \cdot (-6 + 4i) \quad \checkmark$$

$$\rightarrow -12 \cdot (-1) + 20i - 2 \cdot (8i - 8 \cdot (-1) + 6)$$

$$12 + 20i - 2 \cdot (8i + 14)$$

$$12 + 20i - 16i - 28$$

$$-16 + 4i$$

$$a + b \cdot i$$

$$i^4 = i^2 \cdot i^2 = (-1) \cdot (-1) = 1$$

$$i^{13} = i^4 \cdot i^4 \cdot i^4 \cdot i^1 = 1 \cdot 1 \cdot 1 \cdot i = i$$

$$3) \quad \underbrace{-2i}_{\alpha} \cdot \underbrace{(3i-5)^2}_{\beta} \cdot \underbrace{2}_{\gamma} - 4 \cdot \underbrace{(3i-1)}_{\alpha} \cdot \underbrace{(-2i)}_{\gamma} \cdot \underbrace{(4+2i)}_{\delta}$$

$$-4i \cdot (3i-5)(3i-5) + 8i \cdot (3i-1) \cdot (4+2i)$$

$$-4i \cdot (9i^2 - 15i - 15i + 25) + 8i \cdot (12i + 6i^2 - 4 - 2i)$$

$$-4i \cdot (16 - 30i) + 8i \cdot (-10 + 10i)$$

$$-64i + 120i^2 - 80i + 80i^2 = -200 - 144i$$

$$(2i-3) : (3i+1) = \frac{2i-3}{3i+1} \cdot \frac{3i-1}{3i-1} = \frac{-6 - 2i - 9i + 3}{(3i)^2 - 1}$$

$$(3i+1)^2 = (3i)^2 + 2 \cdot 3i \cdot 1 + 1^2 = -8 + 6i \quad \frac{-3 - 11i}{-10} = \frac{-3}{-10} + \frac{-11i}{-10}$$

$$(a+b)(a-b) = a^2 - b^2$$

$$\frac{0\sqrt{x}}{3\sqrt{x}+5}$$

$$0,3 + 1,1i$$

$$\begin{aligned}
\frac{4i - 2}{4 - 3i} \cdot \frac{4 + 3i}{4 + 3i} &= \frac{(4i - 2)(4 + 3i)}{4^2 - (3i)^2} \\
(a - bi) & \quad (a + bi) \\
&= \frac{16i + 12i^2 - 8 - 6i}{16 - (-9)} \\
&= \frac{-20 + 10i}{25} = \frac{-20}{25} + \frac{10i}{25} \\
&= -\frac{4}{5} + \frac{2}{5}i = -0,8 + 0,4i
\end{aligned}$$